

## Optimization of Singkarak hydropower outflow for renewable micro hydropower development

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**Abstract:** The government's initiative to enhance energy resilience and independence include the augmented use of green energy. PLTA Singkarak is a renewable energy facility that harnesses water from Lake Singkarak to operate its turbines, featuring an average tailrace discharge of 30 m<sup>3</sup>/s. The Singkarak Hydroelectric Power Plant receives its energy from PLN's Singkarak Substation, utilizing a 5 MVA transformer for distribution to meet its own consumption needs. Consequently, each month, the Singkarak Hydroelectric Power Plant must diminish its total kWh output by its own use, averaging 4,127.8 kW each day. A small-scale Micro Hydro power plant will be developed to utilize the potential water source at the outflow of the Singkarak Hydroelectric Power Plant, serving as the primary supply for the facility and so decreasing the company's performance target for its own consumption. A sufficiently big outflow tailrace discharge is likely to be repurposed for a micro-hydropower plant. The initial elevation of the Singkarak Hydroelectric Power Plant tailrace exit is 71 meters above sea level, whereas the end elevation is 67 meters above sea level, according to hand measurements. A micro-hydropower plant (PLTMH) can be engineered with a net head of 3.8 m and a flow rate of 10,618 m<sup>3</sup>/s, yielding a maximum power output of 327.8 kW. The turbine employed is a Kaplan turbine, while the generator utilized is a 3-phase synchronous generator, with both components functioning at 1000 rpm. This PLTMH design can supplant the self-consumption of the Singkarak hydropower plant (PLTA), hence enhancing the system's energy efficiency.

**Keywords:** *hydroelectric, tailrace, hydropower, turbine, generator*

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### INTRODUCTION

The increased utilization of green energy is the government's effort to maintain energy resilience and independence (Upadhyay et al., 2024). This study will discuss the potential of green energy in Indonesia, specifically in the West Sumatra region, particularly in Asam Pulau, Kecamatan 2 x 11 Enam Lingsuang, Padang Pariaman Regency. In that area, there is potential energy from the residual water usage or Outflow from the electricity consumption of the Singkarak Hydroelectric Power Plant, as well as the disposal location adjacent to the flow from Batang Anai. The Singkarak Hydroelectric Power Plant is one of the hydroelectric power plants under the auspices of PT PLN (Persero) UPK Bukittinggi with a maximum capacity of 4 x 43.5 MW. The Singkarak Hydroelectric Power Plant utilizes water from Lake Singkarak as the main material to rotate the turbines with an average inflow of 50 m<sup>3</sup>/s and an average outflow of 30 m<sup>3</sup>/s.

In order to support the optimal operation of Common equipment at the Singkarak Hydroelectric Power Plant, the Singkarak Hydroelectric Power Plant utilizes Power Supply directly from PLN electricity,

namely GI Singkarak, as the main supply for the Control Building. The recording of KWh transactions is carried out on the 1st of each month between the GI Singkarak staff and the PLTA Singkarak operation staff as an attachment to the monthly report.

Based on the potential water resources found in the outflow of the Singkarak Hydroelectric Power Plant, a small-scale power generation (Micro Hydro) has been designed to become the main supply for the Singkarak Hydroelectric Power Plant, thereby reducing the company's performance target for Self-Consumption (Gallego-Castillo et al., 2021).

This research, introduces an analytical methodology for assessing the capacity of run-of-river power plants to optimize energy production and economic profitability (Alonso-Travesset et al., 2022). He employs a miniature hydroelectric power facility in Italy to illustrate its potential as a design instrument (Shahzad et al., 2022). This model offers insights into the hydrological and economic regulation of optimal plant capacity, aiding in the identification of policy initiatives to bridge the disparity between economic and energy optimization of run-of-river plants (Yuvaraj et al., 2025). The run-of-river system for medium size can manage disturbances such as garbage, however mini-hydro employs a penstock because to the longer channel compared to medium-scale hydro (Basso & Botter, 2012).

In this article, the discussion is about Planning Complexity, covering technical, environmental, social, and economic factors that must be considered (Lu et al., 2022). Stages of the Hydroelectric Power Plant Project, such as feasibility studies, preliminary design, risk assessment, and implementation (Johri et al., 2025). Similarly, there are planning constraints, namely uncertainties related to location, water availability, construction costs, and government regulations (Bradley et al., 2016).

The article titled evaluates the impact of cost overruns on hydropower projects within Canada's electricity generation strategy (Babaei et al., 2022). It uses the GCAM (Global Change Assessment Model), which includes an endogenous representation of hydropower to analyze its role relative to other renewable energy sources (Vilotijević et al., 2021). Hydropower's Current Role: Hydropower contributes around 60% of Canada's and is projected to grow as part of renewable energy goals (Zhironkin et al., 2023). However, the economic viability of these projects is challenged by frequent cost overruns (Shi et al., 2024).

This research stands at the intersection of technical, ecological, and climate issues (Daramola et al., 2023). Scientific literacy on this topic indicates that the future success of RoR plants in the alpine region heavily depends on technological adaptation to climate change, a deep understanding of ecological flow requirements, and the implementation of energy policies that support sustainability (Hanna & Gross, 2021).

## METHOD

For the data collection technique, we conducted field observations to understand the characteristics of the Singkarak Hydroelectric Power Plant's outflow and the environmental conditions around the Tailrace flow.

The data processing technique used systematic calculations and trial-and-error methods based on Layman's Hydropower Handbook.

1. To determine water discharge, based on Chezy and Manning:

$$Q = A \times V \quad (1)$$

Where Q is the water discharge (m<sup>3</sup>/s), A is the river cross-section (m<sup>2</sup>), and V is the water velocity (m/s).

2. Potential Water Power

For potential water power, we use the formula:

$$P = \eta_{turbine} \times \eta_{generator} \times \rho \times g \times H \times Q \quad (2)$$

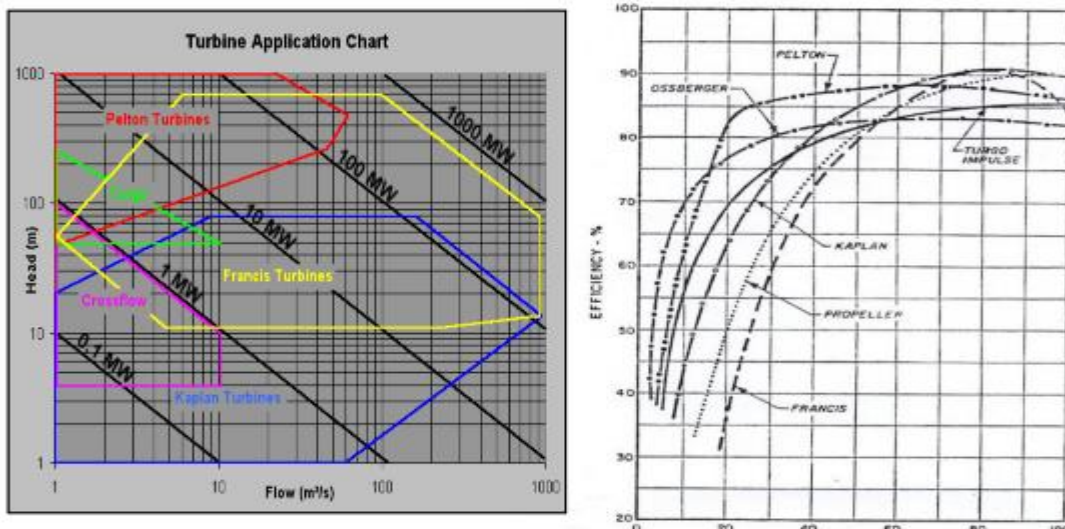
Where P is the power generation capacity (Watts),  $\rho$  is the water density (1000 kg/m<sup>3</sup>), g is the gravitational acceleration (9.81 m/s<sup>2</sup>), H is the height difference from the forebay to the turbine center (m), and Q is the water discharge (m<sup>3</sup>/s). As seen in Figure 1, we conducted measurements of water discharge and head at the PLTA Singkarak discharge location.



**Figure 1. The process of measuring the depth of the Outflow at Singkarak Hydroelectric Power Plant**

To calculate how much capacity is needed for self-consumption, we need to calculate how much energy is produced per hour each month over a period of 5 months (Lombardi et al., 2024). For the specifications of the turbine and generator to be used in the planning of this SHP, we use an approach method based on the guidelines from Layman's (Refdinal et al., 2016).

How to develop a small hydro power plant, Europe 1990 , and the efficiency graph for selecting the type of turbine can be seen in Figure 2.



**Figure 2. How to develop a small hydro power plant, Europe 1990 , and the efficiency graph for selecting the type of turbine**

## FINDINGS AND DISCUSSION

### Monitoring Distributed Energy

This channeled energy is highly relevant in research because it affects the sustainability and efficiency of various energy technologies we use (Trahan & Hess, 2022). Understanding the workings, conversion, and efficiency of energy distribution can help us improve systems and develop more environmentally friendly and efficient energy sources (Martínez-Pérez et al., 2023). Energy consumption profiles need to monitor energy usage patterns, including peak and low loads, to assist in the management and planning of more efficient energy distribution (Zhang & Liu, 2025). This is done to determine how much energy used at a certain time can help optimize the system to reduce excess capacity or supply shortages (Markom et al., 2022). The monitoring of the transmitted energy can be seen and efficient energy sources (El-Madany et al., 2012). The monitoring of the transmitted energy can be seen in table 1.

**Table 1. Hydrological data for the month of July**

PLTA SINGKARAK (4X43,75 MW) SWC= 1,584 M3 /KWH											
INFLOW			OUT FLOW				ELVEJER	DEK HAJAR	P & W	PRODUKSI	
SELOH	DAMBU	TOTAL	TAL. RACE	BANTARI	IND. GATE	TOTAL	Majd	mm	KWH	KWH	
m3/d	m3/d	m3	m3/d	m3/d	m3/d	m3	21	26	27	28	
5,811	47,33	4.089.050	55,33	5,1	0,00	5.223.050	362,13	-	3.947	3.019.198	
5,325	12,59	1.087.924	46,86	5,1	0,00	4.488.924	362,10	-	4.074	3.205.179	
5,325	20,04	1.731.713	54,31	5,1	0,00	5.132.713	362,07	-	3.961	2.962.167	
4,853	10,07	869.958	44,32	5,1	0,00	4.269.958	362,04	2	4.002	2.417.499	
7,711	41,60	3.594.619	49,62	5,1	0,00	4.727.619	362,03	2	3.640	2.706.426	
8,259	56,72	4.900.677	64,73	5,1	0,00	6.033.677	362,02	-	3.877	3.530.958	
7,892	40,73	3.518.971	74,97	5,1	0,00	6.917.971	361,99	-	3.933	4.089.224	
6,999	10,45	902.545	70,89	5,1	0,00	6.565.545	361,94	-	4.007	3.866.733	
6,143	12,16	1.050.895	59,48	5,1	0,00	5.579.895	361,90	-	3.968	3.244.479	
5,811	61,06	5.275.924	42,86	5,1	0,00	4.143.924	361,91	10	4.006	2.337.932	
4,853	54,37	4.697.863	36,16	5,1	0,00	3.564.863	361,92	3	3.775	1.972.363	
4,395	69,94	6.042.515	51,73	5,1	0,00	4.910.515	361,93	12	3.873	2.821.891	
0,000	54,13	4.676.636	49,03	5,1	0,00	4.676.636	361,93	-	3.818	2.674.240	
10,575	50,03	4.322.937	44,93	5,1	0,00	4.322.937	361,93	-	3.841	2.450.945	
6,999	62,87	5.432.242	57,77	5,1	0,00	5.432.242	361,93	-	3.873	3.151.264	
5,325	12,70	1.097.350	60,02	5,1	0,00	5.626.350	361,89	-	3.904	3.273.867	
4,853	1,50	129.809	48,80	5,1	0,00	4.656.809	361,85	-	3.880	2.661.723	
4,546	6,73	581.489	40,92	5,1	0,00	3.976.489	361,82	-	3.847	2.232.228	
4,099	19,09	1.649.785	40,19	5,1	0,00	3.912.785	361,80	-	3.797	2.192.011	
3,810	17,79	1.537.367	38,97	5,0	0,00	3.799.367	361,78	-	3.741	2.125.863	
3,810	24,06	2.078.935	58,33	5,0	0,00	5.471.935	361,75	-	3.734	3.181.777	
3,528	12,90	1.114.730	47,17	5,0	0,00	4.507.730	361,72	-	3.746	2.573.062	
3,118	3,02	261.044	44,32	5,0	0,00	4.260.956	361,68	-	3.777	2.417.270	
3,118	12,00	1.036.455	46,34	4,9	0,00	4.427.455	361,65	-	3.743	2.527.838	
2,726	2,71	233.788	37,04	4,9	0,00	3.623.788	361,62	-	3.790	2.020.472	
2,475	27,09	2.340.400	48,39	4,9	0,00	4.600.400	361,60	-	4.195	2.639.202	
5,008	22,71	1.961.920	43,99	4,9	0,00	4.220.920	361,58	-	4.236	2.399.631	
4,546	22,60	1.952.354	43,88	4,9	0,00	4.211.354	361,56	-	4.137	2.393.592	
4,099	15,02	1.298.151	49,38	4,9	0,00	4.686.151	361,53	-	4.149	2.693.338	
3,810	10,79	932.375	45,17	4,8	0,00	4.319.375	361,50	-	4.182	2.463.969	
3,389	1,81	156.288	36,21	4,8	0,00	3.543.288	361,47	-	4.097	1.975.106	
2,986	4,78	412.992	0,00	4,8	0,00	412.992	0,00	-	-	0	
151,21	818,59		1032,16	188,76	-	146.838.621,71		29,0	121.844	84.221.387	

This hydrological data was collected over a period of 3 months, namely July, August, and September. In the data above, the flow rate at the tailrace is 54.35 m<sup>3</sup>/s with an energy output of 84,221,387 KWh. If the average is calculated from these three months, the flow rate is 44.5 m<sup>3</sup>/s. Therefore, the design flow rate taken is 20 m<sup>3</sup>/s.

### Monitoring KWh Transactions

Electricity payment tariffs are the costs charged to customers for the use of electrical energy (Zhu et al., 2024). These tariffs are determined based on several factors, such as the amount of electricity consumption, customer categories, electricity production costs, and the policies of the government and electricity providers in each country or region (Sari et al., 2022).

In Figure 3, the energy data generated in August is shown, where the energy used from the own power plant is seen in the data as 117,447 KWh. This energy data was taken over 5 months, June, July, August, September, October, and the total energy generated is 639,820 KWh.

**Table 2. Monitoring KWh transactions for the month of August**

BERITA ACARA PENGIRIMAN TENAGA LISTRIK DARI PT PLN (PERSERO) PEMBANGKITAN SUMBAGSEL KE PT PLN (PERSERO) P3B SUMATERA							
		No. KITSEL :					
		No. P3BS :					
Bulan : JULI 2021							
PLTA SINGKARAK				<b>SKR/FORM/10.30.1.0</b>			
No.	URAIAN	MU ID	ENERGI (KWH)				KETERANGAN
			DARI PEMBANGKIT	KE PEMBANGKIT	SELISIH	FAKTOR KALI	
1	2	3	4	5	6	7	8=6x7
1	SKRK #1 [VOEST ALPN]	30108642	1.941.392.861	1.922.344.460	19.048.401	1	19.048.401
2	SKRK #2 [VOEST ALPN]	30108641	722.569.459	701.932.007	20.637.452	1	20.637.452
3	SKRK #3 [VOEST ALPN]	30107604	1.905.624.063	1.880.311.072	25.312.991	1	25.312.991
4	SKRK #4 [VOEST ALPN]	30108640	1.789.210.770	1.769.988.227	19.222.543	1	19.222.543
6	PS 20KV [TRAF0 5MVA]	94B956350	82.236.942	82.002.048	234.894	0,5	117.447
<b>JUMLAH PENGIRIMAN ENERGI NETTO</b>							<b>84.103.940</b>
Catatan :							
- Berita Acara akan dikoreksi bila terjadi kesalahan							
- Data pengiriman energi di atas telah mendapat persetujuan dan ditandatangani oleh :							

From the total energy of 639.820 KWh, the daily energy value can be calculated as 4127.8 KWh. From the daily KWh usage of PLTA Singkarak of 4127.8 KWh, the self-consumption of PLTA Singkarak per hour is 222 KW. Therefore, the planned self-generation capacity is 250 KW to replace the self-consumption supply of PLTA Singkarak taken from the Singkarak Substation.

### Planned Discharge Calculation

Based on the measured and calculated data, the planned discharge can be calculated using formula 2.

$$P = \eta_{\text{turbin}} \times \eta_{\text{generator}} \times \rho \times g \times H \times Q$$

$$Q = \frac{P}{\eta_{\text{turbin}} \times \eta_{\text{generator}} \times \rho \times g \times H}$$

$$= \frac{250 \text{ kW}}{0.6 \times 1000 \times 9.81 \times 4} = 10.681 \text{ m}^3/\text{dtk}$$

Therefore, based on the calculations that have been carried out, a discharge of 10.618 m<sup>3</sup>/s, a height (head) of 4 meters, and a planned power of 250 KW were obtained. Thus, according to figure 2, the most suitable turbine for the planning of this micro-hydropower plant is the Kaplan turbine .

## Limitations and Future Work

Upon reevaluation, numerous deficiencies persist in this research, particularly on the investigation of environmental hazards stemming from the discharge of the Singkarak Hydroelectric Power Plant. Consequently, research must be undertaken to guarantee that the use of the outflow preserves a balance between ecological and human requirements. Establish training programs for the community to comprehend micro-hydro technology and enhance their involvement in operations and maintenance (Nguyen et al., 2024). Investigating the integration of micro-hydro with additional renewable energy sources, such as solar or wind, to establish a more stable and sustainable hybrid energy system, with the deployment of smart grid technology to regulate energy supply and demand in the vicinity. It is essential to examine the legal considerations pertaining to the utilization of river water or the byproducts of hydroelectric power plants as an energy source.

## CONCLUSION

Conclusions should answer the objectives of research. Tells how your work advances the field from the present state of knowledge. Without clear conclusions, reviewers and readers will find it difficult to judge the work, and whether or not it merits publication in the proceedings. This research shows that the outflow from the Singkarak Hydroelectric Power Plant has the potential to be utilized as a micro-hydro energy source, which is an innovative solution to improve water use efficiency. It can provide an efficient alternative for generating electricity from renewable energy sources. The sustainable development of renewable energy, by utilizing existing water flows without requiring large additional infrastructure. By utilizing the outflow as an energy source, this research emphasizes the importance of sustainability in water resource management, as well as its contribution to reducing carbon emissions and promoting the use of renewable energy. It is crucial to ensure that the development of renewable energy does not harm the environment. The use of water from this stream can be directly utilized by the local community, both for providing stable electricity and for creating new economic opportunities, such as supporting infrastructure or developing small industries.

## REFERENCES

- Alonso-Travesset, À., Martín, H., Coronas, S., & De La Hoz, J. (2022). Optimization models under uncertainty in distributed generation systems: A review. *Energies*, 15(5), Article 1932. <https://doi.org/10.3390/en15051932>
- Babaei, R., Ting, D. S.-K., & Cariveau, R. (2022). Feasibility and optimal sizing analysis of stand-alone hybrid energy systems coupled with various battery technologies: A case study of Pelee Island. *Energy Reports*, 8, 4747–4762. <https://doi.org/10.1016/j.egy.2022.03.133>
- Basso, S. M. M., & Botter, G. (2012). Streamflow variability and optimal capacity of run-of-river hydropower plants. *Water Resources Research*, 48(10). <https://doi.org/10.1029/2012WR012017>
- Bradley, P., Coke, A., & Leach, M. (2016). Financial incentive approaches for reducing peak electricity demand: Experience from pilot trials with a UK energy provider. *Energy Policy*, 98, 108–120. <https://doi.org/10.1016/j.enpol.2016.07.022>
- Daramola, A. S., Ahmadi, S. E., Marzband, M., & Ikpehai, A. (2023). A cost-effective and ecological stochastic optimization for integration of distributed energy resources in energy networks considering vehicle-to-grid and combined heat and power technologies. *Journal of Energy Storage*, 57, Article 106203. <https://doi.org/10.1016/j.est.2022.106203>
- El-Madany, H. T., Fahmy, F. H., El-Rahman, N. M. A., & Dorrah, H. T. (2012). Optimization and feasibility analysis of satellite earth station power system using HOMER. *TELKOMNIKA (Telecommunication Computing Electronics and Control)*, 10(2), 359–370.
- Gallego-Castillo, C., Heleno, M., & Victoria, M. (2021). Self-consumption for energy communities in Spain: A regional analysis under the new legal framework. *Energy Policy*, 150, Article 112144. <https://doi.org/10.1016/j.enpol.2021.112144>

- Hanna, R., & Gross, R. (2021). How do energy systems model and scenario studies explicitly represent socio-economic, political and technological disruption and discontinuity? Implications for policy and practitioners. *Energy Policy*, 149, Article 111984. <https://doi.org/10.1016/j.enpol.2020.111984>
- Johri, A., Verma, V., & Basu, M. (2025). Optimization and intelligent control in hybrid renewable energy systems incorporating solar and biomass. *Energy Engineering*, 122(5), 1887–1918. <https://doi.org/10.32604/ee.2025.062355>
- Lombardi, G., Cioccolanti, L., Del Zotto, L., Tomassetti, S., & Campana, P. E. (2024). The role of electric vehicles in hybrid solar-based small energy communities. *Energy Conversion and Management*, 321, Article 119074. <https://doi.org/10.1016/j.enconman.2024.119074>
- Lu, Y., Dai, J., Wang, L., Liu, Y., & Wu, C. (2022). The impact of the energy transition on China's economy under the carbon peaking and carbon neutrality goals: A simulation analysis based on the CGE model. *Thermal Science*, 26(5 Part A), 4043–4056. <https://doi.org/10.2298/TSCI2205043L>
- Markom, A. M., Hadri, M. H. A., Yazid, T. Z. M., Yusof, Z. M., Markom, M. A., & Muhammad, A. R. (2022). Electricity generation from renewable energy based on abandoned wind fan. *Indonesian Journal of Electrical Engineering and Computer Science*, 26(1), 1–8. <https://doi.org/10.11591/ijeecs.v26.i1.pp1-8>
- Martínez-Pérez, R., Ríos-Fernández, J. C., Laine-Cuervo, G., Soto-Pérez, F., Rubio-Serrano, F. J., & Gutiérrez-Trashorras, A. J. (2023). Comparative study of energy performance and water savings between hygroscopic and Rankine cycle in a nuclear power plant: Case study of the HTR-10 reactor. *Results in Engineering*, 20, Article 101600. <https://doi.org/10.1016/j.rineng.2023.101600>
- Nguyen, T. H., Paramasivam, P., Dong, V. H., Le, H. C., & Nguyen, D. C. (2024). Harnessing a better future: Exploring AI and ML applications in renewable energy. *JOIV: International Journal on Informatics Visualization*, 8(1), 55–78. <https://doi.org/10.62527/joiv.8.1.2637>
- Refdinal, N., Nurdin, M., & Fitrianto, E. (2016). Voltage profile improvement of the 20 kV Painan distribution system with multiple distributed renewable energy generation. *International Journal of Technology*, 7(1), 26–37.
- Sari, A., Majdi, A., Opulencia, M. J. C., Timoshin, A., Huy, D. T. N., Trung, N. D., Alsaikhan, F., Hammid, A. T., & Akhmedov, A. (2022). New optimized configuration for a hybrid PV/diesel/battery system based on coyote optimization algorithm: A case study for Hotan county. *Energy Reports*, 8, 15480–15492. <https://doi.org/10.1016/j.egy.2022.11.059>
- Shahzad, M., Qadir, A., Ullah, N., Mahmood, Z., Saad, N. M., & Ali, S. S. A. (2022). Optimization of on-grid hybrid renewable energy system: A case study on Azad Jammu and Kashmir. *Sustainability*, 14(10), Article 5757. <https://doi.org/10.3390/su14105757>
- Shi, S., Zhang, Q., Wei, X., Liu, J., Wang, Y., & Xu, Y. (2024). Anti-fragile planning of urban distribution network for survivability improvement. *Electric Power Construction*, 45(1), 56–67. <https://doi.org/10.12204/j.issn.1000-7229.2024.01.006>
- Trahan, R. T., & Hess, D. J. (2022). Will power be local? The role of local power organizations in energy transition acceleration. *Technological Forecasting and Social Change*, 183, Article 121884. <https://doi.org/10.1016/j.techfore.2022.121884>
- Upadhyay, S., Ahmed, I., & Mihet-Popa, L. (2024). Energy management system for an industrial microgrid using optimization algorithms-based reinforcement learning technique. *Energies*, 17(16), Article 3898. <https://doi.org/10.3390/en17163898>
- Vilotijević, V., Karadžić, U., Vujadinović, R., Kovijanić, V., & Božić, I. (2021). An improved techno-economic approach to determination of more precise installed parameter for small hydropower plants. *Water*, 13(17), Article 2419. <https://doi.org/10.3390/w13172419>
- Yuvaraj, T., Thirumalai, M., Dharmalingam, M., Thanikanti, S. B., & Padmanaban, S. (2025). Smart energy management for revenue optimization and grid independence in an Indian RDS. *Energy Conversion and Management: X*, 26, Article 100955. <https://doi.org/10.1016/j.ecmx.2025.100955>
- Zhang, X., & Liu, J. (2025). Distributed power, energy storage planning, and power tracking studies for distribution networks. *Electronics*, 14(14), Article 2833. <https://doi.org/10.3390/electronics14142833>

- Zhironkin, S., Abu-Abed, F., & Dotsenko, E. (2023). The development of renewable energy in mineral resource clusters—The case of the Siberian Federal District. *Energies*, *16*(9), Article 3843. <https://doi.org/10.3390/en16093843>
- Zhu, C., Zhang, Y., Wang, M., Deng, J., Cai, Y., Wei, W., & Guo, M. (2024). Optimization, validation and analyses of a hybrid PV-battery-diesel power system using enhanced electromagnetic field optimization algorithm and  $\varepsilon$ -constraint. *Energy Reports*, *11*, 5335–5349. <https://doi.org/10.1016/j.egy.2024.04.043>